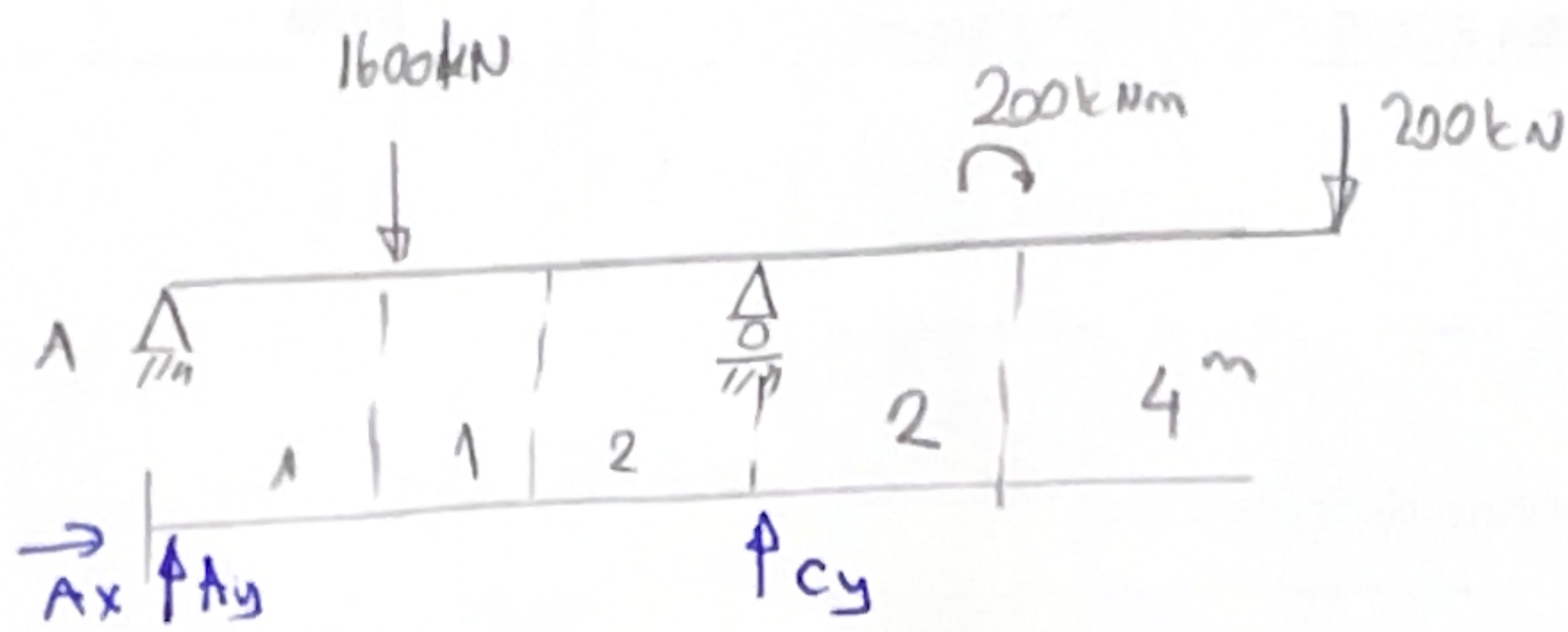


①



$$\sum M_A = 0$$

$$-1600 \cdot 1 + C_y \cdot 4 - 200 - 200 \cdot 10 = 0$$

$$-1600 - 200 - 2000 = -4C_y \Rightarrow 4C_y = 3800 \text{ kN}$$

$$\boxed{C_y = 950 \text{ N}}$$

$$\sum F_y = 0$$

$$A_y + C_y = 1600 + 200 \Rightarrow A_y = 1800 - 950 \Rightarrow \boxed{A_y = 850 \text{ N}}$$

$$\sum F_x = 0$$

$$\boxed{A_x = 0 \text{ N}}$$

②

$$A(0, 0, 5)$$

$$B(0, 3, 0)$$

$$C(6, 3, 0)$$

$$\vec{F}_{AB} = |F_{AB}| \cdot \vec{u}_{AB}$$

$$\vec{AB} = 0\vec{i} + 3\vec{j} - 5\vec{k}$$

$$|\vec{AB}| = \sqrt{9+25} = \sqrt{34} = 5,83$$

$$\vec{u}_{AB} = \frac{3}{5,83}\vec{j} - \frac{5}{5,83}\vec{k}$$

$$\vec{F}_{AB} = 200 \cdot \left[ \frac{3}{5,83}\vec{j} - \frac{5}{5,83}\vec{k} \right]$$

$$\vec{F}_{AB} = 102,9\vec{j} - 171,5\vec{k}$$

$$\vec{F}_{AC} = |F_{AC}| \cdot \vec{u}_{AC}$$

$$\vec{AC} = 6\vec{i} + 3\vec{j} - 5\vec{k}$$

$$|\vec{AC}| = \sqrt{6^2+3^2+5^2} = \sqrt{70} = 8,3$$

$$\vec{u}_{AC} = \frac{6}{8,3}\vec{i} + \frac{3}{8,3}\vec{j} - \frac{5}{8,3}\vec{k}$$

$$\vec{F}_{AC} = 120 \cdot \left[ \frac{6}{8,3}\vec{i} + \frac{3}{8,3}\vec{j} - \frac{5}{8,3}\vec{k} \right]$$

$$\vec{F}_{AC} = 86,7\vec{i} + 43,3\vec{j} - 72,2\vec{k}$$

$$\vec{R} = \vec{F}_{AC} + \vec{F}_{AB} = 86,7\vec{i} + 146,2\vec{j} - 243,7\vec{k}$$





$$|\vec{R}| = \sqrt{(86,7)^2 + (146,2)^2 + (-243,7)^2} = 297,1 \text{ kN}$$

$$b) \cos \alpha = \frac{86,7}{297,1} \Rightarrow \alpha = 73^\circ$$

$$\cos \beta = \frac{-243,7}{297,1} \Rightarrow \beta = 145,17^\circ$$

$$\cos \gamma = \frac{146,2}{297,1} \Rightarrow \gamma = 60,5^\circ$$

③

	x	y	A	xA	yA
	40	20	3200	128000	64000
	60	K	L	36000	28100
	60	50	M	-1176	-980
	30	10	-800	-24000	-8000
			2980	138824	84120
			$\Sigma A$	$\Sigma xA$	$\Sigma yA$

$$\bar{x} = \frac{\Sigma \bar{x}A}{\Sigma A}$$

$$\bar{x} = \frac{138824}{2980} = 46,5 \text{ cm} //$$

$$\bar{y} = \frac{\Sigma \bar{y}A}{\Sigma A}$$

$$\bar{y} = \frac{84120}{2980} = 28,2 \text{ cm} //$$

$$K = 40 + \frac{4 \cdot 20}{3 \cdot \pi} \approx 48,5$$

$$L = \frac{\pi r^2}{2} = \frac{3 \cdot 20^2}{2} \approx 600$$

$$M = \pi r^2 = \pi \cdot (2,5)^2 \approx 19,6$$

④  $100 \cdot 10^6 = 20 \cdot F \Rightarrow \underline{F = 50 \text{ N}}$  //